

# OpenScop

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A Specification and a Library for Data Exchange in Polyhedral Compilation Tools  
Edition 1.0, for OpenScop Specification 1.1 and OpenScop Library 0.9.0  
June 3rd 2014

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This document describes OpenScop, a specification of a file format and a set of data structures for polyhedral compilation tools to talk together. It also describes briefly the OpenScop Library version 0.9.0, a Free Software that provides an example of OpenScop implementation.

It would be quite kind to refer at the present document in any publication that results from the use of the OpenScop Library:

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# 1 Introduction

OpenScop is an open specification that defines a file format and a set of data structures to represent a *static control part* (SCoP for short), i.e., a program part that can be represented in the *polyhedral model*. The goal of OpenScop is to provide a common interface to various polyhedral compilation tools in order to simplify their interaction.

Designing a single format for tools that have different purposes (e.g., as different as code generation and data dependence analysis) may sound strange at first. However we could observe that most available polyhedral compilation tools during the last decade were manipulating more or less the same kind of data (polyhedra, affine functions...) and were actually sharing a part of their input (e.g., iteration domains and context concepts are nearly everywhere). We could also observe that those tools may rely on different internal representations, mostly based on one of the major polyhedral libraries (e.g., Polylib, PPL or isl), and this representation may change over time (e.g., when switching to a more convenient polyhedral library). The OpenScop aim is to provide a stable, unified format that offers a durable guarantee that a tool can use an output or provide an input to another tool without breaking a tool chain because of some internal changes in one element of the chain. The other promise of OpenScop is the ability to assemble or replace the basic blocks of a polyhedral compilation framework at no, or at least low engineering cost.

The policy that drives OpenScop can be summarized by these three rules:

- Embed the *minimum* information to build a complete polyhedral compilation framework in the so-called *core part* (to avoid as much as possible empty or useless information for each tool).
- Provide a *very stable* core part (so users have some guarantee that they will not need to update their tool because of frequent specification evolution),
- Provide a *very flexible* extension part (so it can also be used to test wild new ideas).

Another, more technical, rule may be added:

- Avoid any need for external library or tool to support it (i.e., it's not XML or YAML or anything like that).

The success of OpenScop in meeting its goals totally depends on its acceptance by the tool developers (that have to support it in their tools). To help them, we provide an example implementation: the OpenScop Library. This library (and in particular its API) is not part of the OpenScop specification (which includes only the file format and the set of data structures). It is licensed under the 3-clause BSD license so developers may feel free to use it in their code (either by linking it or copy-pasting its code). This document also describes this library briefly (readers are invited to read at its technical documentation). The current version of the OpenScop Library is still under evaluation, and there is no guarantee that the upward compatibility will be respected, even if we do think so. A lot of reports are necessary to freeze the library API. Thus you are very welcome and encouraged to send reports on bugs, wishes, critics, comments, suggestions or (please!) successful experiences to the OpenScop mailing list [openscop-development@googlegroups.com](mailto:openscop-development@googlegroups.com).

This document is organized as follows. First, we provide some background on the polyhedral model and how it is used to represent and to manipulate programs (see Chapter 2 [Polyhedral Representation], page 3). Next, we describe the OpenScop specification, from the file format (see Section 3.2 [OpenScop File Format Specification], page 18) to the data structures and the OpenScop Library API (see Section 3.3 [OpenScop Data Structure Specification], page 24). Finally we will detail how to install the OpenScop Library (see Section 4.4 [Installation], page 41).



## 2 Polyhedral Representation of Programs

If you are reading at the OpenScop documentation, you probably don't need any explanation about the polyhedral model. It is unlikely that someone will read this paper by mistake. However some vicious advisor may ask their poor engineers/interns/students to work for the very first time on this exciting topic. Most papers on polyhedral compilation are hard to read. Despite my efforts, mine are no exception according to some reviewers. Hence I give there a new try to provide a comprehensive explanation of the polyhedral model without the size and style limits of a classical research paper.

Be aware that to be able to understand the polyhedral model, there are a few prerequisites. You should not read the following while you still ignore what is:

- a `for` loop construction in C programs (do loops in FORTRAN are OK too!),
- an *affine expression*,
- a *vector*,
- a *matrix*,
- a *matrix-vector multiply*.

If you do not know those concepts, please do some search and come back afterwards. And if you are courageous enough, send me a few lines that describe them so I can insert them here!

### 2.1 Motivation: Program Transformations

A direct translation of high level programs written, e.g., in C, to assembly then to object code is likely to produce (very) inefficient applications. Architectures are quite complex, including several levels of cache memory, many cores, deep pipelines, various number of functional units, of registers etc. The list of such "architectural features" is growing with each new generation of processors. To achieve the best performance, the object program must use these features in a smart way. Programmers use high level languages for productivity and portability: typically they do not have to take care of the target architecture but to ensure they write programs which produce the right output. Hence, the problem of mapping the program to the target architecture in the most efficient way is left to the compiler.

The compiler may see a high level program as a specification *of an output*. The program is a list of instructions to be executed to produce the output. As long as the output is guaranteed to be as the programmer specified in his code, the compiler is free to modify the program. For instance, let us imagine we are working on an architecture with only three registers and we consider the following statements written by a programmer:

```
x = a + b;
y = c + d;
z = a * b;
```

It is easy to see that we can reorder the three statements in any way without modifying the semantics (no statement reads or writes a variable that another statement writes). Because of the lack of registers, the solutions such that the first and the third statements are one after the other are better because `a` and `b` will be put in the processor registers by one statement and can be reused directly by the other one without reading from memory (this is called a *data locality improving* transformation). Hence a better statement order is, e.g.:

```
x = a + b;
z = a * b; // a and b are still in processor registers
y = c + d;
```

We can also notice that it is possible to run the three statements in parallel (possibly on different processors). The programmer may explicit this in a way the compiler and/or the

architecture is able to understand. For instance, we can use OpenMP to describe parallelism (this is called a *parallelizing* transformation):

```
#pragma omp parallel sections
{
    #pragma omp section
    {
        x = a + b;
    }
    #pragma omp section
    {
        y = c + d;
    }
    #pragma omp section
    {
        z = a * b;
    }
}
```

However, the right way to optimize this program is probably a tradeoff between these two techniques. This is true if, e.g., the target architecture has some limitations to run too many operations in parallel, or, like in our case, when some data may be reused by some processors. Hence, the best optimization for our small example is probably the following:

```
#pragma omp parallel sections
{
    #pragma omp section
    {
        x = a + b;
        z = a * b;
    }
    #pragma omp section
    {
        y = c + d;
    }
}
```

This example is quite trivial because the statements are executed only once. The real sport begins when we have to deal with loops, as we will see momentarily. However, polyhedral compilation framework users have to be conscious that we *need* to transform programs to achieve the best performance and that the best transformation that has to be discovered (at the price of many, many efforts) and performed may be quite complex. Hence the need of powerful model and tools.

## 2.2 Thinking in Polyhedra

Since the very first compilers, the internal representation of programs is the *Abstract Syntax Tree*, or AST. In such representation, each statement appears only once even if it is executed many times (e.g., when it is enclosed inside a loop). This is a limitation for finding and applying complex transformations:

- It limits program analysis power. For instance if a statement *depends* on another statement (i.e., they access the same memory location and at least one of these accesses is a write), we will consider both statements as unique entities while the dependence relation may involve only few statement executions.



- It limits program transformation power. Loop transformations operate on statement executions. For instance, because they consider all statement executions at the same time, present day production compilers are not able to achieve loop fusion (that tries to merge the loop bodies of two loops) if the loop bounds of the two loops do not match (yes, that's ridiculous).
- It limits program manipulation flexibility. Trees are very rigid data structures that are not easy to manipulate. Program transformation may require very complex transformations that will imply deep modifications of the control flow.

The Polyhedral Model is a convenient alternative representation which combines analysis power, expressiveness and high flexibility. The drawback is it breaks the classical structure of programs that every programmer is familiar with. It requires some (real) efforts to be smoothly manipulated, but it definitely worth it. It is based on three main concepts, *iteration domain*, *scattering function* and *access function* that are described in depth in the following sections.

A program part that can be represented using the Polyhedral Model is called a **Static Control Part** or **SCoP** for short.

### 2.2.1 Iteration Domain

The key aspect of the polyhedral model is to consider *statement instances*. A statement instance is *one* execution of a statement. A statement outside a loop has only one instance while those inside loops may have many. Let us consider the following code with two statements S1 and S2:

```
pi = 3.14;           // S1
for (i = 0; i < 5; i++)
    A[i] = pi;       // S2
```

The list of statement instances is the following (we just have to fully unroll the loop):

```
pi = 3.14;
A[0] = pi;
A[1] = pi;
A[2] = pi;
A[3] = pi;
A[4] = pi;
```

Each instance of a statement which is enclosed inside a loop may be referred thanks to its outer loop counters (or *iterators*). In the polyhedral model we consider statements as functions of the outer loop counters that may produce statement instances: instead of simply "S2", we use preferably the notation S2(i). For instance we denote the statement instance A[3] = pi; of the previous example as S2(3). This means *instance of statement S2 for i = 3*. If a statement S3 is enclosed inside two loops of iterators i (outermost loop) and j (innermost loop), we would denote it S3(i, j), and so on with more enclosing loops.

The ordered list of iterators (ordered from the outermost iterator to the innermost iterator) is called the **iteration vector**. For instance the iteration vector for S3 is (i, j), for S2 it is (i), and for S1 it is empty since it has no enclosing loop: (). A more precise reading at the notation S2(3) would show that it denotes the instance of statement S2 for the iteration vector (2).

Obviously, dealing with statement instances does not mean we have to unroll all loops. First because there would be probably too many instances to deal with, and second because we probably just do not know how many instances there are. For instance in the following loop it is impossible to know (at compile time) how many times the statement S3 will be executed:

```
for (i = 2; i <= N; i++)
    for (j = 2; j <= N; j++)
        A[i] = pi;    // S3
```

Such a loop is said to be *parametric*: it depends on (at least) a value called a *parameter* which is not modified during the execution of the whole loop, but is unknown at compile time. Here, the only parameter is  $N$ .

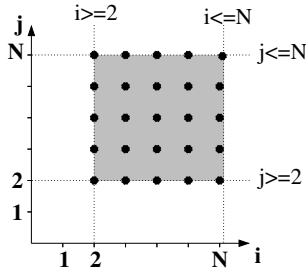
A compact way to represent all the instances of a given statement is to consider the set of all possible values of its iteration vector. This set is called the **iteration domain**. It can be conveniently described thanks to all the constraints on the various iterators the statement depends on. For instance, let us consider the statement **S3** of the previous program. The iteration domain is the set of iteration vectors  $(i, j)$ . Because of the parameter, we are not able to achieve a precise list of all possible values. It would look like this:

$$\begin{array}{cccccc} (2,2) & (2,3) & (2,4) & \dots & (2,N) \\ (3,2) & (3,3) & (3,4) & \dots & (3,N) \\ \dots & \dots & \dots & \dots & \dots \\ (N,2) & (N,3) & (N,4) & \dots & (N,N) \end{array}$$

A better way is to say it is the set of iteration vectors  $(i, j)$  such that  $i$  is an integer greater or equal than 2 and lower or equal than  $N$ , and  $j$  is an integer greater or equal than 2 and lower or equal than  $N$ . This may be written in the following mathematical form:

$$D_{S3} = \{(i, j) \in \mathbb{Z}^2 \mid 2 \leq i \leq N \wedge 2 \leq j \leq N\}$$

It is easy to see that this iteration domain is a part of the 2-dimensional space  $\mathbb{Z}^2$ . We often use in our research papers a graphical representation that gives a better view of this subspace:



Here, the iteration domain is specified thanks to a set of constraints. When those constraints are affine and depend only on the outer loop counters and some parameters, the set of constraints defines a *polyhedron* (more precisely this is a *Z-polyhedron*, but we use *polyhedron* for short). Hence the *polyhedral model*!

To manipulate a set of affine constraints easily, we rely on a matrix representation. To write it, we use the *homogeneous* iteration vector: it is simply the iteration vector with some additional dimensions to represent the parameters and the constant. For instance for the statement **S3**, the iteration vector in homogeneous coordinates is  $(i, j, N, 1)$  (we will now call it *iteration vector* directly for short). Then we write all the constraints as affine inequalities of the form *affine constraint*  $\geq 0$ . For instance for the statement **S3** the set of constraints is:

$$\begin{cases} i - 2 & \geq 0 \\ -i + N & \geq 0 \\ j - 2 & \geq 0 \\ -j + N & \geq 0 \end{cases}$$

Lastly, we translate the constraint system to the form **domain matrix** \* *iteration vector*  $\geq 0$ :

$$\begin{bmatrix} 1 & 0 & 0 & -2 \\ -1 & 0 & 1 & 0 \\ 0 & 1 & 0 & -2 \\ 0 & -1 & 1 & 0 \end{bmatrix} \begin{pmatrix} i \\ j \\ N \\ 1 \end{pmatrix} \geq \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \end{pmatrix}$$

The domain matrix will be used in all our tools to provide the information on the iteration domain of a given statement (the iteration vector is in general an implicit information).

### 2.2.2 Scattering Function

There is no ordering information inside the iteration domain: it only describes the set of statement instances but **not** the order in which they have to be executed relatively to each other. In the past the lexicographic order of the iteration domain was considered, this is no more true (especially when using CLooG). If we do not provide any ordering information, this means that the statement instances may be executed in any order (this is useful, e.g., to specify parallelism). However, some statement instances may depend on some others and it may be critical to enforce a given order (or non-order). Hence we need another information.

We call *scattering* any kind of ordering information in the polyhedral model. There exists many kind of ordering, such as *allocation*, *scheduling*, *chunking* etc. They are all expressed in the same way, i.e., using *logical stamps*, but they may have different semantics.

In the case of **scheduling**, the logical stamps are logical dates that express at which date a statement instance has to be executed. For instance, let us consider the following three statements:

```
x = a + b;    // S1
y = c + d;    // S2
z = a * b;    // S3
```

The scheduling of a statement  $S$  is typically denoted by  $\theta_S$ . Let us consider the following logical dates for each statement:

```
 $\theta_{S1} = 2$ 
 $\theta_{S2} = 3$ 
 $\theta_{S3} = 1$ 
```

It means that statement **S3** has to be executed at logical date 1, statement **S1** has to be executed at logical date 2 and statement **S2** has to be executed at logical date 3. The target code has to respect this scheduling (the order of the logical dates), hence it would look like the following where the variable  $t$  denotes the time:

```
t = 1;
z = a * b;    // S3
t = 2;
x = a + b;    // S1
t = 3;
y = c + d;    // S2
```

When some statements share the same logical date, this means that, once the program reaches this logical date, the two statements can be executed in any order, or better, in parallel. For instance let us consider the following scheduling:

```
 $\theta_{S1} = 1$ 
 $\theta_{S2} = 2$ 
 $\theta_{S3} = 1$ 
```

Statements **S1** and **S3** have the same logical date, moreover, **S2** has a greater logical date than **S1** and **S3**. Hence the target code would be:

```

t = 1;
#pragma omp parallel sections
{
    #pragma omp section
    {
        x = a + b;    // S1
    }
    #pragma omp section
    {
        z = a * b;    // S3
    }
}
t = 2;
y = c + d;          // S2

```

Logical dates may be multidimensional, as clocks: the first dimension may correspond to days (most significant), the next one to hours (less significant), the third to minutes and so on. For instance we can consider the following multidimensional schedules for our example:

$$\begin{aligned}
 \theta_{S1} &= (1, 1) \\
 \theta_{S2} &= (2, 1) \\
 \theta_{S3} &= (1, 2)
 \end{aligned}$$

It is not very hard to decypher the meaning of such scheduling. Because of the first dimension, statements **S1** and **S3** will be executed before statement **S2** (**S1** and **S3** are executed at day 1, while **S2** is executed at day 2). The second dimension is not really useful there for **S2** because it is the only statement executed at day 2. Nevertheless it allows to order **S1** and **S3** relatively to each other since **S1** is executed at hour 1 of day 1 while **S3** is executed at hour 2 of day 1. The corresponding target code is the following, with some additional time variables for a better view of the ordering (**t1** corresponds to the first time dimension, **t2** to the second one):

```

t1 = 1;
t2 = 1;
x = a + b;    // S1
t2 = 2;
z = a * b;    // S3
t1 = 2;
t2 = 1;
y = c + d;    // S2

```

In the case of **allocation** (in the literature we can find some papers calling it *placement*), the logical stamp is a processor number expressing on which processor a statement instance has to be executed. Typically, allocations are written in the same way as scheduling. Here, we denote it  $P_S$  for a statement **S**. For instance, let us consider the following allocation:

$$\begin{aligned}
 P_{S1} &= 1 \\
 P_{S2} &= 2 \\
 P_{S3} &= 1
 \end{aligned}$$

The corresponding target code has to take into account that both statements **S1** and **S3** have to be executed on the same processor (they have the same logical number 1) and that statement **S2** has to be executed on another processor (logical number 2). A possible target code is the following:

```

#pragma omp parallel sections
{
    #pragma omp section
    {
        // Logical processor 1
        x = a + b;    // S1
        z = a * b;    // S3
    }
    #pragma omp section
    {
        // Logical processor 2
        y = c + d;    // S2
    }
}

```

We can note that no order has been specified for the statements **S1** and **S3** that are executed on the same processor. Hence any order is satisfying. For sake of flexibility, it is usual to build a scattering whose various dimensions do not have the same semantics. A typical construction is *space/time mapping* where the first  $n$  dimensions are devoted to allocation, then the last  $m$  dimensions are devoted to scheduling. Typically, space/time mapping is written in the same way as scheduling. Here we denote it  $M_S$  for a statement **S**. For instance, let us consider the following space/time mapping for our example where one dimension is devoted to mapping and one dimension is devoted to scheduling:

$$\begin{aligned}
 M_{S1} &= (1, 2) \\
 M_{S2} &= (2, 1) \\
 M_{S3} &= (1, 1)
 \end{aligned}$$

Here we have the same first dimension as the previous example, thus the allocation of the statements to processors is the same. The second dimension precises on a given processor at which logical date a statement instance has to be executed. Here, the statement **S1** is executed at day 2 on processor 1 while the statement **S3** is executed at day 1 onto the same processor. It follows this space/time mapping corresponds to the following target code (we added an additional variable to represent the local logical clocks):

```

#pragma omp parallel sections
{
    #pragma omp section
    {
        // Logical processor 1
        t = 1;
        z = a * b;    // S3
        t = 2;
        x = a + b;    // S1
    }
    #pragma omp section
    {
        // Logical processor 2
        t = 1;
        y = c + d;    // S2
    }
}

```

For the same reason as discussed for iteration domains (see Section 2.2.1 [Iteration Domain], page 5), it is not possible to define a scattering for each statement instance, especially if the

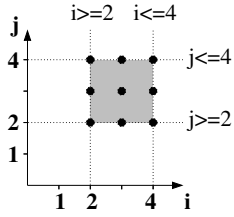
statement belongs to a (possibly parametric) loop. The iteration vector fully defines an instance of a given statement. Thus, a practical way to provide a scattering for each instance of a given statement is to use a *function* that depends on the iteration vector. In this way the function may associate to each iteration vector a different scattering. We call these functions **scattering functions**. Scattering functions are *affine* functions of the outer loop counter and the global parameters. For instance, let us consider the following source code:

```
for (i = 2; i <= 4; i++)
  for (j = 2; j <= 4; j++)
    P[i+j] += A[i] + B[j]; // S4
```

The iteration domain of the statement S4 is:

$$D_{S4} = \{(i, j) \in \mathbb{Z}^2 \mid 2 \leq i \leq 4 \wedge 2 \leq j \leq 4\}.$$

If you are still not comfortable with the mathematical notation, it corresponds to the following graphical representation:



The list of the statement instances of S4 (the integer points of its iteration domain) corresponds to the following iteration vectors:

```
iteration vector
(2,2)
(2,3)
(2,4)
(3,2)
(3,3)
(3,4)
(4,2)
(4,3)
(4,4)
```

Let us suppose we want to schedule the instances of the statement S4 (the integer points of its iteration domain) using the following scheduling function:

$$\theta_{S4}(i, j) = (j + 2, 3 * i + j)$$

We only need to apply the function to each iteration vector to find the logical date of each instance:

| iteration vector |     | logical date |
|------------------|-----|--------------|
| (2,2)            | --> | (4,8)        |
| (2,3)            | --> | (5,9)        |
| (2,4)            | --> | (6,10)       |
| (3,2)            | --> | (4,11)       |
| (3,3)            | --> | (5,12)       |
| (3,4)            | --> | (6,13)       |
| (4,2)            | --> | (4,14)       |
| (4,3)            | --> | (5,15)       |
| (4,4)            | --> | (6,16)       |

The polyhedral model users do not have to take care about the generation of a target code that respects the scattering: the CLooG<sup>1</sup> tool is there to solve the problem quite easily. For the previous example, the target code would be the following (**t1** and **t2** correspond to the two dimensions of the logical date, the reader may take care that this code actually implements the scattering function):

```

for (t1 = 4; t1 <= 6; t1++) {
  for (t2 = t1+4; t2 <= t1+10; t2++) {
    if ((-t1+t2+2)%3 == 0) {
      i = (-t1+t2+2)/3 ;
      j = t1-2 ;
      P[i+j] += A[i] + B[j]; // S4
    }
  }
}

```

Obviously with such a twisted scheduling, it is hard to see the "meaning" of the transformation. To name any kind of program transformation as a magic spell ("tile", "fuse", "skew"...) is an old bad habit which is not relevant anymore in the polyhedral model: a scheduling may be an arbitrary complex sequence of basic-old-good transformations. Nevertheless it is most of the time quite easy to translate well known transformations to schedules. For instance, let us consider this new scheduling function:

$$\theta_{S4}(i, j) = (j, i)$$

Using CLooG, we can generate the target code:

```

for (t1 = 2; t1 <= 4; t1++) {
  for (t2 = 2; t2 <= 4; t2++) {
    i = t2;
    j = t1;
    P[i+j] += A[i] + B[j]; // S4
  }
}

```

It is easy to see (and analyze) that it corresponds to a classical *loop interchange* transformation.

A very useful example of multi-dimensional scattering functions is the **scheduling of the original program**. The method to compute it is quite simple (see [Fea92], page 47). The idea is to build an abstract syntax tree of the program and to read the scheduling for each statement. For instance, let us consider the following implementation of a Cholesky factorization:

```

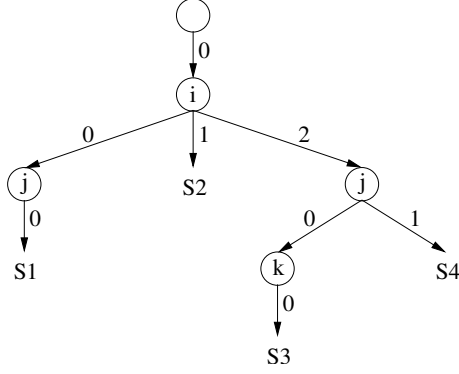
/* A Cholesky factorization kernel. */
for (i=1;i<=N;i++) {
  for (j=1;j<=i-1;j++) {
    a[i][i] -= a[i][j] ;           // S1
  }
  a[i][i] = sqrt(a[i][i]) ;       // S2
  for (j=i+1;j<=N;j++) {
    for (k=1;k<=i-1;k++) {
      a[j][i] -= a[j][k]*a[i][k] ; // S3
    }
    a[j][i] /= a[i][i] ;           // S4
  }
}

```

---

<sup>1</sup> <http://www.cloog.org>

The corresponding abstract syntax tree is shown in the following figure. It directly gives the scattering functions (schedules) for all the statements of the program (just follow the paths).



$$\begin{cases} \theta_{S1}(i, j) &= (0, i, 0, j, 0) \\ \theta_{S2}(i) &= (0, i, 1) \\ \theta_{S3}(i, j, k) &= (0, i, 2, j, 0, k, 0) \\ \theta_{S4}(i, j) &= (0, i, 2, j, 1) \end{cases}$$

These schedules depend on the iterators and give for each instance of each statement a unique execution date. Using such scattering functions allows CLoog to re-generate the input code.

To easily manipulate the scattering function of any statement  $S$ , we translate it to the matrix form:  $\theta_S(\text{iteration vector}) = \mathbf{scattering\ matrix} * \text{iteration vector}$ . For instance let us consider again our previous example  $\theta_{S4}(i, j) = (j + 2, 3 * i + j)$ . We write it in the following way:

$$\theta_{S4} \begin{pmatrix} i \\ j \\ 1 \end{pmatrix} = \begin{bmatrix} 0 & 1 & 2 \\ 3 & 1 & 0 \end{bmatrix} \begin{pmatrix} i \\ j \\ 1 \end{pmatrix}$$

**The scattering matrix will be used in all our tools to provide the information on the scattering of a given statement (the iteration vector is in general an implicit information).**

### 2.2.3 Access Function

Before applying any transformation, it is essential to deeply analyze both the original program and the transformation to ensure the transformation does not imply any modification of the original program semantics. In the polyhedral model, we are able to achieve an exact analysis when all the memory accesses are made through arrays (note that variables are a particular case of arrays since they are simply arrays with only one memory location) with affine subscripts that depend on outer loop counters and global parameters (note that *subscripts* are sometimes called *index* or *accesses* in the literature).

For instance let us consider the array access  $A[2*i+j][j][i+N]$ . It has three dimensions, each subscript dimension is an affine form of some outer loop iterators ( $i$  and  $j$ ) and global parameters ( $N$ ) hence it corresponds to an acceptable array access to be analyzed in the polyhedral model.

Each array access can target a different memory cell depending on the statement instance, i.e., depending on the iteration vector. Thus we use access functions (or subscript functions, or index functions, as you prefer to call it) depending on the iteration vector to describe an array access. In our example, the access function would be written  $F_A(i, j) = (2 * i + j, j, i + N)$ .

To easily manipulate the access function of any array  $A$ , we translate it to the matrix form:  $F_A(\text{iteration vector}) = \mathbf{access\ matrix} * \text{iteration vector}$ . For instance let us consider again our



previous example. We would write it in the following way:

$$F_A \begin{pmatrix} i \\ j \\ N \\ 1 \end{pmatrix} = \begin{bmatrix} 2 & 1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 1 & 0 \end{bmatrix} \begin{pmatrix} i \\ j \\ N \\ 1 \end{pmatrix}$$

**The access matrix will be used in all our tools to provide the information on the access of a given statement (the iteration vector is in general an implicit information).**

## 2.3 What's Next?

OK, now you have an idea about how we do represent a program part in the polyhedral model. You know the three main concepts, namely: domain, scattering and access. What can you do with this?! Well, pretty much anything related to code restructuring! The core idea will be to rely on the mathematical representation to extract useful information about your code (data reuse, parallelism...) and to generate a scattering to benefit from the properties you analysed. However, OpenScop's documentation is not the right place to learn at this (OpenScop is all about representation, not about manipulation). Probably it is the right time for you to have a look at:

- PoCC <http://pocc.sourceforge.net>
- Pluto <http://pluto-compiler.sourceforge.net>

Have fun :-) !



## 3 OpenScop Specification

OpenScop provides an explicit polyhedral representation of a static control part. It has been designed by various polyhedral compilation tool writers from various institutions. It builds on previous popular polyhedral file and data structure formats (such as *.cloog* and CLoog data structures) to provide a unique, extensible format to most polyhedral compilation tools. It is composed of two parts. The first part, the so-called *core part*, is devoted to the polyhedral representation of a SCoP. It contains what is strictly necessary to build a complete source-to-source framework in the polyhedral model and to output a semantically equivalent code for the SCoP, from analysis to code generation. The second part of the format, the so-called *extension part*, contains extensions to provide additional informations to some tools.

### 3.1 Preliminary Example

OpenScop is a specification for representing static control program parts in the polyhedral model. Thus, we can translate some code parts to an equivalent OpenScop representation. As an example, let us consider the following matrix-multiply kernel:

```
#pragma scop
if (N > 0) {
  for (i = 0; i < N; i++) {
    for (j = 0; j < N; j++) {
      C[i][j] = 0.0;
      for (k = 0; k < N; k++)
        C[i][j] = C[i][j] + A[i][k] * B[k][j];
    }
  }
}
```

The Clan<sup>1</sup> tool may be used to translate this code part to an OpenScop representation automatically. The `#pragma scop` is used here for Clan, but some other tool may not need it. Here is the result of the translation to an OpenScop textual representation.

#### DON'T PANIC

Explanations will follow and it is not as cryptic as it seems to be !

```
<OpenScop>

# ===== Global
# Backend Language
C

# Context
CONTEXT
1 3 0 0 0 1
# e/i | N | 1
  1    1   -1   ## N-1 >= 0

# Parameter names are provided
1
# Parameter names
```

---

<sup>1</sup> <http://www.lri.fr/~bastoul/development/clan/>

```

<strings>
N
</strings>

# Number of statements
2

# ===== Statement 1
# Number of relations describing the statement
3

# ----- 1.1 Domain
DOMAIN
4 5 2 0 0 1
# e/i | i    j    | N    | 1
    1    1    0    0    0    ## i >= 0
    1   -1    0    1   -1    ## -i+N-1 >= 0
    1    0    1    0    0    ## j >= 0
    1    0   -1    1   -1    ## -j+N-1 >= 0

# ----- 1.2 Scattering
SCATTERING
5 10 5 2 0 1
# e/i | s1    s2    s3    s4    s5    | i    j    | N    | 1
    0   -1    0    0    0    0    0    0    0    0    ## s1 = 0
    0    0   -1    0    0    0    1    0    0    0    ## s2 = i
    0    0    0   -1    0    0    0    0    0    0    ## s3 = 0
    0    0    0    0   -1    0    0    1    0    0    ## s4 = j
    0    0    0    0    0   -1    0    0    0    0    ## s5 = 0

# ----- 1.3 Access
WRITE
3 8 3 2 0 1
# e/i | Arr  [1]  [2]  | i    j    | N    | 1
    0   -1    0    0    0    0    0    1    ## C
    0    0   -1    0    1    0    0    0    ## [i]
    0    0    0   -1    0    1    0    0    ## [j]

# ----- 1.4 Statement Extensions
# Number of Statement Extensions
1
<body>
# Number of original iterators
2
# Original iterator names
i j
# Statement body expression
C[i][j] = 0.0;
</body>

# ===== Statement 2
# Number of relations describing the statement

```

5

# ----- 2.1 Domain

DOMAIN

6 6 3 0 0 1

| # | e/i | i  | j  | k  | N | 1  |                |
|---|-----|----|----|----|---|----|----------------|
|   | 1   | 1  | 0  | 0  | 0 | 0  | ## i >= 0      |
|   | 1   | -1 | 0  | 0  | 1 | -1 | ## -i+N-1 >= 0 |
|   | 1   | 0  | 1  | 0  | 0 | 0  | ## j >= 0      |
|   | 1   | 0  | -1 | 0  | 1 | -1 | ## -j+N-1 >= 0 |
|   | 1   | 0  | 0  | 1  | 0 | 0  | ## k >= 0      |
|   | 1   | 0  | 0  | -1 | 1 | -1 | ## -k+N-1 >= 0 |

# ----- 2.2 Scattering

SCATTERING

7 13 7 3 0 1

| # | e/i | s1 | s2 | s3 | s4 | s5 | s6 | s7 | i | j | k | N | 1 |           |
|---|-----|----|----|----|----|----|----|----|---|---|---|---|---|-----------|
|   | 0   | -1 | 0  | 0  | 0  | 0  | 0  | 0  | 0 | 0 | 0 | 0 | 0 | ## s1 = 0 |
|   | 0   | 0  | -1 | 0  | 0  | 0  | 0  | 0  | 1 | 0 | 0 | 0 | 0 | ## s2 = i |
|   | 0   | 0  | 0  | -1 | 0  | 0  | 0  | 0  | 0 | 0 | 0 | 0 | 0 | ## s3 = 0 |
|   | 0   | 0  | 0  | 0  | -1 | 0  | 0  | 0  | 0 | 1 | 0 | 0 | 0 | ## s4 = j |
|   | 0   | 0  | 0  | 0  | 0  | -1 | 0  | 0  | 0 | 0 | 0 | 0 | 1 | ## s5 = 1 |
|   | 0   | 0  | 0  | 0  | 0  | 0  | -1 | 0  | 0 | 0 | 1 | 0 | 0 | ## s6 = k |
|   | 0   | 0  | 0  | 0  | 0  | 0  | 0  | -1 | 0 | 0 | 0 | 0 | 0 | ## s7 = 0 |

# ----- 2.3 Access

WRITE

3 9 3 3 0 1

| # | e/i | Arr | [1] | [2] | i | j | k | N | 1 |        |
|---|-----|-----|-----|-----|---|---|---|---|---|--------|
|   | 0   | -1  | 0   | 0   | 0 | 0 | 0 | 0 | 1 | ## C   |
|   | 0   | 0   | -1  | 0   | 1 | 0 | 0 | 0 | 0 | ## [i] |
|   | 0   | 0   | 0   | -1  | 0 | 1 | 0 | 0 | 0 | ## [j] |

READ

3 9 3 3 0 1

| # | e/i | Arr | [1] | [2] | i | j | k | N | 1 |        |
|---|-----|-----|-----|-----|---|---|---|---|---|--------|
|   | 0   | -1  | 0   | 0   | 0 | 0 | 0 | 0 | 1 | ## C   |
|   | 0   | 0   | -1  | 0   | 1 | 0 | 0 | 0 | 0 | ## [i] |
|   | 0   | 0   | 0   | -1  | 0 | 1 | 0 | 0 | 0 | ## [j] |

READ

3 9 3 3 0 1

| # | e/i | Arr | [1] | [2] | i | j | k | N | 1 |        |
|---|-----|-----|-----|-----|---|---|---|---|---|--------|
|   | 0   | -1  | 0   | 0   | 0 | 0 | 0 | 0 | 2 | ## A   |
|   | 0   | 0   | -1  | 0   | 1 | 0 | 0 | 0 | 0 | ## [i] |
|   | 0   | 0   | 0   | -1  | 0 | 0 | 1 | 0 | 0 | ## [k] |

READ

3 9 3 3 0 1

| # | e/i | Arr | [1] | [2] | i | j | k | N | 1 |        |
|---|-----|-----|-----|-----|---|---|---|---|---|--------|
|   | 0   | -1  | 0   | 0   | 0 | 0 | 0 | 0 | 3 | ## B   |
|   | 0   | 0   | -1  | 0   | 0 | 0 | 1 | 0 | 0 | ## [k] |

```

0    0    0   -1    0    1    0    0    0    ##    [j]

# ----- 1.4 Statement Extensions
# Number of Statement Extensions
1
<body>
# Number of original iterators
3
# Original iterator names
i j k
# Statement body expression
C[i][j] = C[i][j] + A[i][k] * B[k][j];
</body>

# ===== Extensions
<comment>
May the power of the polyhedral model be with you.
</comment>

</OpenScop>

```

We will not describe here precisely the structure and the components of this output, this is described in depth in a further section (see Section 3.2 [OpenScop File Format Specification], page 18). This format has been designed to be a possible input or output file format of most of polyhedral compilation tools. If you read the description of the polyhedral representation of programs, you should already feel familiar with this file format (see Chapter 2 [Polyhedral Representation], page 3).

## 3.2 OpenScop File Format Specification

The following grammar describes the structure of the OpenScop file format where terminals are preceeded by "\_". Except stated otherwise, there can be at most one terminal per line in the file. Moreover, each line may finish with a comment, starting by the '#' character. Each relevant part will be explained in more details momentarily:

```

OpenScop      ::= Start_tag Data End_tag
Start_tag     ::= "<OpenScop>"
End_tag       ::= "</OpenScop>"
Data          ::= Context Statements Extension_list
Context       ::= Language Parameter_Domain Parameters
Statements    ::= Nb_statements Statement_list
Statement_list ::= Statement Statement_list | (void)
Relation_list ::= _Relation Relation_list | (void)
Extension_list ::= _Generic Extension_list | (void)
Statement     ::= Statement_relations Statement_extensions
Statement_extensions ::= Num_Extensions Extension_list
Parameters    ::= "0" | "1" Parameter_information
Statement_relations ::= Nb_relations Relation_List
Parameter_domain ::= _Relation
Language      ::= _String
Nb_Relations  ::= _Integer
Num_extensions ::= _Integer
Parameter_information ::= _Generic

```

The ‘**Context**’ and the ‘**Statements**’ parts compose the *core part*, i.e., what is strictly necessary to build a complete source to source framework based on OpenScop:

- ‘**Context**’ represents the global information of the SCoP. It consists on the target language, the global constraints on the parameters and optionally the parameter information which may be necessary for the code generation process. The constraints on the parameters are represented as a relation (see Section 3.2.1.2 [Context Domain Relation], page 22). The parameter information is optional. It is preceded by a boolean which precises whether it is provided or not. It is a generic information (see Section 3.2.2 [Generics], page 23), a **strings** (see Section 3.2.2.1 [Strings Generic], page 23) for instance.
- ‘**Statements**’ represents the information about the statements. ‘**Nb\_statements**’ is the number of statements in the SCoP, i.e. the number of ‘**Statement**’ items in the ‘**Statement\_list**’. ‘**Statement**’ represents the information on a given statement. To each statement is associated a list of relations and, optionally, a list of statement extensions. The list of relations may include one iteration domain (see Section 3.2.1.1 [Iteration Domain Relation], page 20), one scattering relation (see Section 3.2.1.3 [Scattering Relation], page 22) and several access relations (see Section 3.2.1.4 [Access Relation], page 22). There is no mandatory ordering, but for consistency reason it would be much appreciated that iteration domain comes first (if present) then scattering (if present), then accesses (if present). The statement extensions is an optional information. It starts with a integer which precises the number of extensions provided. It is generic information (see Section 3.2.2 [Generics], page 23), a **body** (see Section 3.2.2.2 [Body Generic], page 23) for instance.

The ‘**Extension\_list**’ represents the *extension part* and may contain an arbitrary number of generic informations (see Section 3.2.2 [Generics], page 23). Few examples of possible extensions are presented in a further section (see Section 3.4 [Extensions], page 30).

As shown by the grammar, the input file describes the various pieces of information based on strings, integers, *relations* and *generics*. Relations and Generics are specific to OpenScop and are described in depth in the following Sections (see Section 3.2.1 [Relations], page 19, and see Section 3.2.2 [Generics], page 23).

### 3.2.1 Relations

*Relations* are the essence of the OpenScop format and contain the "polyhedral" information. They are used to describe either an iteration domain, or a context domain, or a scattering or a memory access.

We use the relation term as a shortcut to denote a union of convex relations, each element of the union being described by a set of constraints in an extended PolyLib format (see [Wil93], page 47). The number of elements in the union is given by an integer on the first line, optionally followed by a comment starting with ‘#’. This number of elements can be omitted when there is only one element. Each element in the union has the following syntax:

1. Some optional comment lines beginning with ‘#’.
2. A line with the type of the relation, possibly followed by comments. The type can be one of the following:
  - **UNDEFINED**: generic relation,
  - **CONTEXT**: for context information,
  - **DOMAIN**: for iteration domains,
  - **SCATTERING**: for scattering relation,
  - **READ**: for read accesses,
  - **WRITE**: for write accesses,

- MAY\_WRITE: for may-write accesses,
3. A line with 6 numbers, possibly followed by comments:
    1. the number of rows of the constraint matrix,
    2. the number of columns of the constraint matrix,
    3. the number of *output dimensions*,
    4. the number of *input dimension*,
    5. the number of *local dimensions* (existentially quantified dimensions),
    6. the number of *parameters*.

The sum of the last four numbers should be equal to the number of columns minus two. The remaining two columns are the equality/inequality indicator and the constant term. The number of parameters should be the same for all relations in the entire OpenScop file or data structure.

4. The constraint rows. Each row corresponds to a constraint the relation has to satisfy. Each row must be on a single line and is possibly followed by comments. The constraint is an equality  $p(x) = 0$  if the first element is 0, an inequality  $p(x) \geq 0$  if the first element is 1. The next elements are the coefficients of the output dimensions, followed by coefficients of the input dimensions, the existentially quantified dimensions and finally the parameters. The last element is the constant term.

This representation is the basis for several purposes. Examples for iteration domains (see Section 3.2.1.1 [Iteration Domain Relation], page 20), context domains (see Section 3.2.1.2 [Context Domain Relation], page 22), scattering relations (see Section 3.2.1.3 [Scattering Relation], page 22) and access relations (see Section 3.2.1.4 [Access Relation], page 22) are provided in further sections.

### 3.2.1.1 Iteration Domain Relation

Iteration domain represents the set of instances of the corresponding statement. OpenScop iteration domains are represented as relations with the following conventions:

- the type is DOMAIN,
- there is 0 input dimension,
- loop iterators correspond to output dimensions.

For instance, assuming that ‘i’, ‘j’ and ‘k’ are the loop iterators and ‘M’ and ‘N’ are the parameters, the domain defined by the following constraints :

$$\begin{cases} -i + M & \geq 0 \\ -j + N & \geq 0 \\ i + j - k & \geq 0 \end{cases}$$

can be written in the input file as follows:

```
# This is an iteration domain
DOMAIN
1 # Number of relations in the union
3 7 3 0 0 2 # 3 rows, 7 cols: 3 output dims and 2 params
# e/i | i j k | M N | 1
1 -1 0 0 1 0 0 # -i + M >= 0
1 0 -1 0 0 1 0 # -j + N >= 0
1 1 1 -1 0 0 0 # i + j - k >= 0
```



Equivalently, it can be written in the following way as the number of relations in the union can be omitted if it is 1:

```
# This is an iteration domain
DOMAIN
3 7 3 0 0 2          # 3 rows, 7 cols: 3 output dims and 2 params
# e/i| i   j   k | M   N | 1
  1  -1   0   0   1   0   0 #   -i + M >= 0
  1   0  -1   0   0   1   0 #   -j + N >= 0
  1   1   1  -1   0   0   0 # i + j - k >= 0
```

As an example for unions, let us consider the following pseudo-code:

```
for (i = 1; i <= N; i++) {
  if ((i >= M) || (i <= 2*M))
    S1(i);
}
```

The iteration domain of ‘S1’ can be divided into two relations and written in the OpenScop file as follows:

```
# This is an iteration domain
DOMAIN
2 # Number of relations in the union
# Union part No.1
3 5 1 0 0 2          # 3 rows, 5 cols: 1 output dim and 2 params
# e/i| i | M   N | 1
  1   1   0   0  -1 #   i >= 1
  1  -1   0   1   0 #   i <= N
  1   1  -1   0   0 #   i >= M
# Union part No.2
3 5 1 0 0 2          # 3 rows, 5 cols: 1 output dim and 2 params
# e/i| i | M   N | 1
  1   1   0   0  -1 #   i >= 1
  1  -1   0   1   0 #   i <= N
  1  -1   2   0   0 #   i <= 2*M
```

As an example for local dimensions (existentially quantified dimensions), let us consider the following pseudo-code:

```
for (i = 1; i <= N; i++) {
  if ((i % 2) == 0)
    S1(i);
}
```

The iteration domain of ‘S1’ is composed of all even integer values between 1 and N. The "divisible by two" constraint can be expressed as follows: there exists an integer ‘ld’ such that ‘i = 2\*ld’. We encode this thanks to a new local dimension:

```
# This is an iteration domain
DOMAIN
3 5 1 0 1 1          # 3 rows, 5 cols: 1 output dim, 1 local dim, 1 param
# e/i| i |ld | N | 1
  0   1  -2   0   0 #   i = 2*ld
  1   1   0   0   1 #   i >= 1
  1  -1   0   1   0 #   i <= N
```

### 3.2.1.2 Context Domain Relation

The context domain is a particular case of iteration domain (see Section 3.2.1.1 [Iteration Domain Relation], page 20) where there are only constraints about parameters (no loop iterators). Hence it is the same as an iteration domain, with the following conventions:

- the type is **CONTEXT**,
- there is 0 input dimension,
- there is 0 output dimension.

### 3.2.1.3 Scattering Relation

Scattering relation maps an iteration domain to a logical time and/or space (and/or) anything. OpenScop scattering information is represented as relations (see Section 3.2.1 [Relations], page 19) with the following conventions:

- the type is **SCATTERING**,
- output dimensions correspond to scattering dimensions,
- loop iterators correspond to input dimensions.

As an example of a scattering relation and assuming that ‘i’, ‘j’ and ‘k’ are the loop iterators and ‘M’ and ‘N’ are the parameters, take for instance:  $\theta_S(i, j, k) = (j + 2, 3 * i + j, k + N + 1)$ . We can represent it in the following way:

```
# A scattering relation
SCATTERING
# 3 rows, 10 columns: 3 scattering dimensions, 3 iterators, 2 parameters
3 10 3 3 0 2
# e/i | s1  s2  s3 | i   j   k | M   N | 1
  0  -1   0   0   0   1   0   0   0   2 # s1 = j+2
  0   0  -1   0   3   1   0   0   0   0 # s2 = 3*i+j
  0   0   0  -1   0   0   1   0   1   1 # s3 = k+N+1
```

### 3.2.1.4 Access Relation

Access relation maps an iteration domain to an array space. Each array accessed in the SCoP has a unique identification number. OpenScop relation information is represented as relations (see Section 3.2.1 [Relations], page 19) with the following conventions:

- the type is one of the following:
  - **READ**, for read accesses,
  - **WRITE**, for write accesses,
  - **MAY\_WRITE**, for may write accesses,
- output dimensions correspond to the array identifier and dimensions,
- the first output dimension corresponds to the array identifier,
- the (i+1)th output dimension corresponds to the ith array dimension (i>1),
- loop iterators correspond to input dimensions.

As an example of a scattering relation and assuming that ‘i’, ‘j’ and ‘k’ are the loop iterators and ‘M’ and ‘N’ are the parameters, let us consider the array access `A[2*i+j][j][i+N]` (the identifier of A is 42), and let us suppose this is a read access. Its representation would be the following:

```

# A read access relation
READ
# 4 rows, 11 columns: 4 array dimensions, 3 iterators, 2 parameters
4 11 4 3 0 2
# e/i|Arr [1] [2] [3]| i   j   k | M   N | 1
  0  -1   0   0   0   0   0   0   0   0  42  # A
  0   0  -1   0   0   2   1   0   0   0   0  # [2*i+j]
  0   0   0  -1   0   0   1   0   0   0   0  # [j]
  0   0   0   0  -1   1   0   0   0   1   0  # [i+N]

```

To understand this representation, consider that OpenScop accesses are general memory accesses and not array accesses. The memory is seen as a big array `Mem` while usual array names correspond to the first dimension. Hence our example translates to `Mem[42] [2*i+j] [j] [i+N]`.

Unions of access relations are allowed. In this case, each union part must refer at the same array identifier, and the number of dimensions must be consistent.

### 3.2.2 Generics

*Generics* represent any elaborated non-polyhedral information in the OpenScop format. They are used to represent the parameter information, the statement body information as well as the extensions. Each generic information is delimited using XML-like tags corresponding to its URI (Unique Resource Identifier), For instance, if the generic has the URI `foo`, the begin tag is `<foo>` and the end tag is `</foo>`.

Two generics, namely `strings` (see Section 3.2.2.1 [Strings Generic], page 23) and `body` (see Section 3.2.2.2 [Body Generic], page 23) are part of the OpenScop specification to provide the minimum, stricly necessary information to build a complete source-to-source polyhedral framework based on OpenScop. However, generics can be basically *anything* as long as they are properly delimited. OpenScop implementations will simply ignore non-supported generics and warn the user with the mention of the non-supported URIs. Support of new generics will be added throught the extension mechanism.

#### 3.2.2.1 Strings Generic

The purpose of the `strings` generic is to represent a list of textual strings on one line (which may be used, e.g., to represent the list of parameter names in the order used in the relation). Its URI is `strings` and its file format respects the following grammar:

```

Strings_generic    ::= "<strings>" Strings "</strings>"
Strings            ::= _String String_list | (void)

```

A possible example of textual `strings` is the following:

```

<strings>
Not one sentence but 6 strings!
</strings>

```

#### 3.2.2.2 Body Generic

The purpose of the `body` generic is to represent the textual information about a statement. It contains the number of original iterators on the first line, the list of original iterators on the second line (the loop counters of the statement surrounding loops in the original program) and the original textual body expression on the third line. Its URI is `body` and its file format respects the following grammar (the `String` rule is reused, see Section 3.2.2.1 [Strings Generic], page 23):

```

Body_generic       ::= "<body>" Body "</body>"
Body               ::= Nb_iterators Iterator_list Expression
Nb_iterators       ::= _Integer
Iterator_list      ::= Strings

```

Expression ::= Strings

A possible example of textual body is the following:

```
<body>
# Number of original iterators
2
# Original iterators
i j
# Original statement expression
A[i+j] += B[i] * C[j];
</body>
```

### 3.3 OpenScop Data Structure Specification

The OpenScop specification offers a small set of C data structures devoted to represent a SCoP in memory in a convenient way. Using them in some tool or library may greatly facilitate its interaction with other tools or libraries which rely on this representation as well. Every field may not be useful for a given tool or library. A general rule for all the data structure is that a NULL pointer or a -1 integer value means the information is not present. Contrary to engineering time, memory is cheap today, so it's much probably not a big deal that some fields are left empty. Every field may not be enough for a given tool or library. In this case it is much recommended to provide a new extension which may be reused by other users (see Section 3.4 [Extensions], page 30).

Each tool or library may have its own implementation of the OpenScop data structures. The type names should not be the same as those provided as an example here (they correspond to the OpenScop Library implementation). The names of the fields, and their ordering, should however be the same. In this way, the interaction between tools and libraries should be as simple as a cast.

Before reading at the OpenScop data structures, it is much recommended to read at the OpenScop file format description, as it is quite close to this representation (see Section 3.2 [OpenScop File Format Specification], page 18).

#### 3.3.1 osl\_int\_t

```
union osl_int {
    long int  sp;           /* Single precision int */
    long long dp;          /* Double precision int */
    void*     mp;           /* Pointer to a multiple precision int */
};
typedef union osl_int  osl_int_t;
typedef union osl_int* osl_int_p;
```

The `osl_int_t` union stores an integer element. The union is used to implement the multiple precision support of OpenScop. A given implementation may or may not support a given precision type. However, dedicated functions or macros must tell the user whether a given precision type is supported or not. The `mp` field is a pointer to a multiple precision int, e.g., a `mpz_t` from the GNU GMP library.

### 3.3.2 `osl_relation_t`

```

struct osl_relation {
    int type; /* What this relation is encoding */
    int precision; /* Precision of the matrix elements */
    int nb_rows; /* Number of rows */
    int nb_columns; /* Number of columns */
    int nb_output_dims; /* Number of output dimensions */
    int nb_input_dims; /* Number of input dimensions */
    int nb_local_dims; /* Number of local dimensions */
    int nb_parameters; /* Number of parameters */
    osl_int_t** m; /* Matrix of constraints */
    void* usr; /* User-managed field */
    struct osl_relation* next; /* Next relation in the union */
};
typedef struct osl_relation osl_relation_t;
typedef struct osl_relation* osl_relation_p;

```

The `osl_relation_t` structure stores a part of an union of relations. A union of relation is a NULL-terminated linked list of union parts (`next` field). The `type` field may provide some information about what the relation is encoding:

- -1: undefined (`OSL_UNDEFINED`),
- 2: context domain (`OSL_TYPE_CONTEXT`),
- 3: iteration domain (`OSL_TYPE_DOMAIN`),
- 4: scattering relation (`OSL_TYPE_SCATTERING`),
- 6: read access relation (`OSL_TYPE_READ`),
- 7: write access relation (`OSL_TYPE_WRITE`),
- 8: may write access relation (`OSL_TYPE_MAY_WRITE`),

The various numbers provide the details on the relation itself (see Section 3.2.1 [Relations], page 19) while the `m` field points to the constraint matrix. The precision of the constraint matrix elements is provided by the `precision` field. It can take the following values:

- 32: 32 bits precision, elements are long int (`OSL_PRECISION_SP`),
- 64: 64 bits precision, elements are long long int (`OSL_PRECISION_DP`),
- 0: multiple precision, elements are GNU GMP Library's `mpz_t` (`OSL_PRECISION_MP`).

Finally, the `usr` field is provided for user's convenience.

### 3.3.3 `osl_relation_list_t`

```

struct osl_relation_list {
    osl_relation_p elt; /* Element of the list */
    struct osl_relation_list* next; /* Next element of the list */
};
typedef struct osl_relation_list osl_relation_list_t;
typedef struct osl_relation_list* osl_relation_list_p;

```

The `osl_relation_list_t` structure is a NULL-terminated linked list of `osl_relation_t` data structures. `elt` is a relation element of the list and `next` is the pointer to the next element of the list.

### 3.3.4 `osl_interface_t`

```
typedef void (*osl_idump_f) (FILE*, void*, int);
typedef char* (*osl_sprint_f)(void*);
typedef void* (*osl_sread_f) (char*);
typedef void* (*osl_malloc_f)();
typedef void (*osl_free_f) (void*);
typedef void* (*osl_clone_f) (void*);
typedef int (*osl_equal_f) (void*, void*);

struct osl_interface {
    char* URI; /* Unique interface identifier string */
    osl_idump_f idump; /* Pointer to the idump function */
    osl_sprint_f sprint; /* Pointer to the sprint function */
    osl_sread_f sread; /* Pointer to the sread function */
    osl_malloc_f malloc; /* Pointer to the malloc function */
    osl_free_f free; /* Pointer to the free function */
    osl_clone_f clone; /* Pointer to the clone function */
    osl_equal_f equal; /* Pointer to the equal function */
    struct osl_interface* next; /* Next interface in the list */
};
typedef struct osl_interface osl_interface_t;
typedef struct osl_interface* osl_interface_p;
```

The `osl_interface_t` structure represents a node in a NULL-terminated list of interfaces. Each node stores the *interface* of a generic OpenScop object, i.e., its unique name (URI) and the function pointers to all the base functions it has to provide. Extension providers will find information relative to those functions in the OpenScop Library description (see Section 4.2 [Base Functions], page 39) and the section dedicated to writing extensions (see Section 4.6.4 [Extension Development], page 44).

### 3.3.5 `osl_generic_t`

```
struct osl_generic {
    void* data; /* Pointer to some data */
    osl_interface_p interface; /* Interface to work with the data */
    struct osl_generic* next; /* Pointer to the next generic */
};
typedef struct osl_generic osl_generic_t;
typedef struct osl_generic* osl_generic_p;
```

The `osl_generic_t` structure represents a node in a NULL-terminated list of generic elements. It stores some data and operations with no pre-defined type. The information is accessible through the `data` pointer while the type and operations are accessible through the `interface` pointer. It is used to represent data that are allowed to differ in implementations, such as symbols and extensions.

### 3.3.6 `osl_strings_t`

```
struct osl_string {
    char** string; /* NULL-terminated array of strings */
};
typedef struct osl_strings osl_strings_t;
typedef struct osl_strings* osl_strings_p;
```

The `osl_strings_t` structure represents a NULL-terminated list of C character strings. It is encapsulated into a structure to allow its manipulation through a generic type.

### 3.3.7 `osl_body_t`

```

struct osl_body {
    osl_strings_p iterators;    /* Original iterators */
    osl_strings_p expression;  /* Original statement expression */
};
typedef struct osl_body  osl_body_t;
typedef struct osl_body* osl_body_p;

```

The `osl_body_t` structure stores a statement body in a textual form. The complete original expression (directly copy-pasted from the original code) is in the expression field while the textual forms of the original iterators are in the iterators field. They may be used for substitutions inside the expression.

### 3.3.8 `osl_statement_t`

```

struct osl_statement {
    osl_relation_p domain;      /* Iteration domain */
    osl_relation_p scattering;  /* Scattering relation */
    osl_relation_list_p access; /* List of array access relations */
    osl_generic_p extension;    /* Generic extensions */
    void* usr;                  /* A user-defined field */
    struct osl_statement* next; /* Next statement in the list */
};
typedef struct osl_statement  osl_statement_t;
typedef struct osl_statement* osl_statement_p;

```

The `osl_statement_t` structure represents a node in a NULL-terminated linked list of statements. Each node contains the useful information for a given statement to process it within a polyhedral framework. The order in the list may matter for naming conventions (e.g. "S1" for the first statement in the list). The iteration domain and the scattering are represented using an `osl_relation_p` structure while the accesses are using a list of relations: one for each memory access in the statement. The extensions part is a list of generics `osl_generic_t` which can contain useful structures such as `body`. The `body` field should provide information about the statement body (since it has a generic type, the specification is not strict about how it is used), e.g., using the `osl_body_t` data structure (see Section 3.3.7 [`osl_body_t`], page 27). It is also possible to use the `usr` field, but it has to be totally managed by the user.

### 3.3.9 `osl_scop_t`

```

struct osl_scop {
    int version;                /* Version of the data structure */
    char* language;             /* Target language */
    osl_relation_p context;     /* Constraints on the parameters */
    osl_generic_p parameters;   /* Information about parameters */
    osl_statement_p statement;  /* Statement list */
    osl_interface_p registry;   /* Registered extension interfaces */
    osl_generic_p extension;    /* Extension list */
    void* usr;                  /* A user-defined field */
    struct osl_scop* next;     /* Next scop in the list */
};
typedef struct osl_scop  osl_scop_t;
typedef struct osl_scop* osl_scop_p;

```

`osl_scop_t` represents a node in a NULL-terminated list of scops. It stores the useful informations of a static control part of a program to process it within a polyhedral framework. To

prepare OpenScop specification evolution, the **version** field tells the version of the data structure. It should be set to 1 for now (and hopefully a very, very, long time). First, it contains the informations about the context. The target language is expressed in the **language** field. The constraints on the global parameters are detailed in the **context** field. The **parameters** field should provide information about the parameters (since it has a generic type, the specification is not strict about how it is used), e.g., using the **osl\_strings\_t** data structure (see Section 3.3.6 [osl\_strings\_t], page 26). Finally, it contains the list of statements **statement**, the list of registered interfaces for generic types **registry** and the list of extensions **extension**. It is also possible to use the **usr** field, but it has to be totally managed by the user.

As an example, let us consider again the matrix multiply program (see Section 3.1 [Preliminary Example], page 15). The next figure gives a possible representation in memory for this SCoP thanks to the OpenScop data structures (it has been actually printed by the **osl\_scop\_dump** function), note that symbols like parameters, original iterators and statement expression are represented with an **osl\_strings\_t** which does not belong to the specification but to the OpenScop Library implementation:

```

+-- osl_scop_t
| |
| | Version: 1
| |
| | Language: C
| |
| | +-- osl_relation_t (CONTEXT, 32 bits)
| | | 1 3 0 0 0 1
| | | [ 1 1 -1 ]
| | |
| | +-- osl_generic_t
| | |
| | | +-- osl_interface_t: URI = strings
| | |
| | | +-- osl_strings_t: N
| | |
| |
| | +-- osl_statement_t (S1)
| | |
| | | +-- osl_relation_t (DOMAIN, 32 bits)
| | | | 4 5 2 0 0 1
| | | | [ 1 1 0 0 0 ]
| | | | [ 1 -1 0 1 -1 ]
| | | | [ 1 0 1 0 0 ]
| | | | [ 1 0 -1 1 -1 ]
| | |
| | | +-- osl_relation_t (SCATTERING, 32 bits)
| | | | 5 10 5 2 0 1
| | | | [ 0 -1 0 0 0 0 0 0 0 0 ]
| | | | [ 0 0 -1 0 0 0 1 0 0 0 ]
| | | | [ 0 0 0 -1 0 0 0 0 0 0 ]
| | | | [ 0 0 0 0 -1 0 0 1 0 0 ]
| | | | [ 0 0 0 0 0 -1 0 0 0 0 ]
| | |
| | | +-- osl_relation_list_t
| | |

```



```

| | | | | +-- osl_relation_t (WRITE, 32 bits)
| | | | | 3 8 3 2 0 1
| | | | | [ 0 -1 0 0 0 0 0 0 1 ]
| | | | | [ 0 0 -1 0 1 0 0 0 0 ]
| | | | | [ 0 0 0 -1 0 1 0 0 0 ]
| | | | |
| | | | |
| | | | | +-- osl_generic_t
| | | | | |
| | | | | +-- osl_interface_t: URI = body
| | | | | |
| | | | | +-- osl_strings_t: i j
| | | | | |
| | | | | +-- osl_strings_t: C[i][j] = 0.0;
| | | | | |
| | | | |
| | | | | V
| | | | | osl_statement_t (S2)
| | | | | |
| | | | | +-- osl_relation_t (DOMAIN, 32 bits)
| | | | | | 6 6 3 0 0 1
| | | | | | [ 1 1 0 0 0 0 0 ]
| | | | | | [ 1 -1 0 0 1 -1 ]
| | | | | | [ 1 0 1 0 0 0 ]
| | | | | | [ 1 0 -1 0 1 -1 ]
| | | | | | [ 1 0 0 1 0 0 ]
| | | | | | [ 1 0 0 -1 1 -1 ]
| | | | | |
| | | | | +-- osl_relation_t (SCATTERING, 32 bits)
| | | | | | 7 13 7 3 0 1
| | | | | | [ 0 -1 0 0 0 0 0 0 0 0 0 0 0 0 ]
| | | | | | [ 0 0 -1 0 0 0 0 0 1 0 0 0 0 0 ]
| | | | | | [ 0 0 0 -1 0 0 0 0 0 0 0 0 0 0 ]
| | | | | | [ 0 0 0 0 -1 0 0 0 0 1 0 0 0 0 ]
| | | | | | [ 0 0 0 0 0 -1 0 0 0 0 0 0 1 ]
| | | | | | [ 0 0 0 0 0 0 -1 0 0 0 1 0 0 ]
| | | | | | [ 0 0 0 0 0 0 0 -1 0 0 0 0 0 ]
| | | | | |
| | | | | +-- osl_relation_list_t
| | | | | |
| | | | | +-- osl_relation_t (WRITE, 32 bits)
| | | | | | 3 9 3 3 0 1
| | | | | | [ 0 -1 0 0 0 0 0 0 1 ]
| | | | | | [ 0 0 -1 0 1 0 0 0 0 ]
| | | | | | [ 0 0 0 -1 0 1 0 0 0 ]
| | | | | |
| | | | | V
| | | | | osl_relation_list_t
| | | | | |
| | | | | +-- osl_relation_t (READ, 32 bits)
| | | | | | 3 9 3 3 0 1
| | | | | | [ 0 -1 0 0 0 0 0 0 1 ]

```



preferred way to write the extension body. Extensions in an OpenScop data structure must be accessible through one pointer. This pointer will be stored in the `data` field of an `osl_generic_t` container (see Section 3.3.5 [osl\_generic\_t], page 26). There must be only one extension with the same URI in an OpenScop file or data structure.

Extension writers may write a short documentation about their extension to be added to this document. For consistency reason, this documentation should comply to the documentation of the `comment` option (see Section 3.4.1 [Comment Extension], page 31). To describe the file format, it is allowed to reuse the existing rules and terminals present in the OpenScop file format description without defining them (see Section 3.2 [OpenScop File Format Specification], page 18). By sending a documentation, you accept it to be added to this document. In particular, the sender fully accepts the license and copyright notice.

### 3.4.1 Comment Extension

#### Description

- URI: `comment`.
- Author: Cédric Bastoul <cedric.bastoul@u-psud.fr>.
- Purpose: the `comment` extension stores a textual string.

#### File Format

The `comment` extension file format respects the following grammar:

```
Comment_generic    ::= "<comment>" Comment "</comment>"
Comment            ::= _Text
```

An example of textual `comment` extension is the following:

```
<comment>
This is a comment string.
</comment>
```

#### Data Structure

The `comment` extension data structure is the following:

```
struct osl_comment {
    char* comment; /* Comment message as a 0-terminated string */
};
typedef struct osl_comment osl_comment_t;
typedef struct osl_comment* osl_comment_p;
```

### 3.4.2 Scatnames Extension

#### Description

- URI: `scatnames`.
- Author: Cédric Bastoul <cedric.bastoul@u-psud.fr>.
- Purpose: the `scatnames` extension provides a list of textual scattering dimension names.

#### File Format

The `scatnames` extension file format respects the following grammar. It reuses the `Strings` description (see Section 3.2.2.1 [Strings Generic], page 23):

```
Scatnames_generic  ::= "<scatnames>" Scatnames "</scatnames>"
Scatnames          ::= Strings
```

The list of scattering dimension names is provided on one single line. The names are separated with spaces. A possible example of such an extension is the following:

```

<scatnames>
# List of scattering dimension names:
beta_0 i beta_1 j beta_2
</scatnames>

```

### Data Structure

The `scatnames` extension data structure is the following:

```

struct osl_scatnames {
    osl_strings_p names; /* List of textual scattering dimension names. */
};
typedef struct osl_scatnames osl_scatnames_t;
typedef struct osl_scatnames* osl_scatnames_p;

```

The order of the scattering dimension names in the list corresponds to the order of the scattering dimensions.

## 3.4.3 Arrays Extension

### Description

- URI: arrays.
- Author: Cédric Bastoul <cedric.bastoul@u-psud.fr>.
- Purpose: the `arrays` extension provides a set of textual array names corresponding to the array identifiers used in the access relations.

### File Format

The `arrays` extension file format respects the following grammar:

```

Arrays_generic      ::= "<arrays>" Arrays "</arrays>"
Arrays              ::= Nb_items Item_list
Item_List           ::= Item Item_list | (void)
Item                ::= Identifier Name
Nb_items            ::= _Integer
Identifier           ::= _Integer
Name                ::= _String

```

The number of array names is provided on the first line, then each following line contains a couple identifier-name. For instance, the following example is a correct textual `arrays` extension. It corresponds to the array names of the preliminary example (see Section 3.1 [Preliminary Example], page 15):

```

<arrays>
# Number of array names:
3
1 C # Identifier 1 corresponds to array name "C"
3 B # Identifier 3 corresponds to array name "B"
2 A # Identifier 2 corresponds to array name "A"
</arrays>

```

### Data Structure

The `arrays` extension data structure is the following:

```

struct osl_arrays {
    int nb_names; /* Number of names */
    int * id; /* Array of nb_names identifiers */
    char** names; /* Array of nb_names names */
};
typedef struct osl_arrays osl_arrays_t;
typedef struct osl_arrays* osl_arrays_p;

```

Each name has a name string and an identifier: the  $i$ th name has name string `names[i]` and identifier `id[i]`.

### 3.4.4 Coordinates Extension

#### Description

- URI: `coordinates`.
- Author: Cédric Bastoul <cedric.bastoul@u-psud.fr>.
- Purpose: the `coordinates` extension provides the information about the SCoP location in the original code: the original file name/path, the starting and ending lines of the SCoP in this file (inclusives) and the indentation level.

#### File Format

The `coordinates` extension file format respects the following grammar:

```
Coordinates_generic ::= "<coordinates>" Coordinates "</coordinates>"
Coordinates          ::= File_name Start_line Start_column
                        End_line End_column Indentation
File_name             ::= _String
Start_line            ::= _Integer
Start_column          ::= _Integer
End_line              ::= _Integer
End_column            ::= _Integer
Indentation           ::= _Integer
```

The original file name where the SCoP has been extracted is provided on the first line, then the starting line and column numbers of the SCoP, then the ending line and column numbers of the SCoP, and lastly the indentation level (the number of spaces characters each line of the SCoP starts with). For instance, the following example is a correct textual `coordinates` extension:

```
<coordinates>
# File name
./test/ax-do.c
# Starting line and column
9 3
# Ending line and column
15 4
# Indentation
2
</coordinates>
```

#### Data Structure

The `coordinates` extension data structure is the following:

```
struct osl_coordinates {
    char* name; /* File name */
    int start; /* First line of the SCoP in the source file */
    int end; /* Last line of the SCoP in the source file */
    int indent; /* Indentation */
};
typedef struct osl_coordinates osl_coordinates_t;
typedef struct osl_coordinates* osl_coordinates_p;
```

### 3.4.5 Clay Extension

#### Description

- URI: `clay`.

- Author: Cédric Bastoul <cedric.bastoul@u-psud.fr>.
- Purpose: the `clay` extension stores a Clay script.

### File Format

The `clay` extension file format respects the following grammar:

```
Clay_generic      ::= "<clay>" Clay "</clay>"
Clay              ::= _Text
```

An example of a `clay` extension is the following:

```
<clay>
fission([2,1], 1);
stripmine([2], 32, 1);
unroll([3], 4);
</clay>
```

### Data Structure

The `clay` extension data structure is the following:

```
struct osl_clay {
    char* script; /* Clay script as a 0-terminated string */
};
typedef struct osl_clay osl_clay_t;
typedef struct osl_clay* osl_clay_p;
```

## 3.4.6 Extbody Extension

### Description

- URI: `extbody`.
- Author: Joel Poudroux <joel.poudroux@u-psud.fr>.
- Purpose: the `extbody` extension provides a list of coordinates to locate each access easily in the body string.

### File Format

The `extbody` extension file format respects the following grammar. It reuses the `Body` description (see Section 3.2.2.2 [Body Generic], page 23)

```
Extbody_generic  ::= "<extbody>" Extbody "</extbody>"
Extbody          ::= Coordinate_number Coordinate_list Body
Coordinate_list  ::= Access_start Access_length Coordinate_list | (void)
Coordinate_number ::= _Integer
Access_start     ::= _Integer
Access_length    ::= _Integer
```

This extension extends the see Section 3.2.2.2 [Body Generic], page 23. The number of accesses `Coordinate_number` must be equal to the number of access relations in the statement. Each coordinate is associated with the corresponding access relation in the access relation list (the order matters). It is possible that an access has two relations in the access relation list (when it is in read/write mode). In this case we can replace one of the couple of coordinates with a `(-1 -1)`. It is possible to put twice the same coordinates, but using `(-1 -1)` may improve some tool efficiency (e.g., Clay would apply twice the same processing otherwise). For each access, `Access_start` is the index of this acces in the body string (starting from 0), and `Access_length` is the length of the access text. For instance:

```

<extbody>
# Number of access
3
# Mapping start/length
0 1 # a coordinates (read)
-1 -1 # a coordinates (write)
6 9 # b coordinates
# Number of original iterators
0
# Statement body expression
a++ + b[i+1][j];
</extbody>

```

### Data Structure

The extbody extension data structure is the following:

```

struct osl_extbody {
    osl_body_p body;
    int nb_access;    /**< Nb of access. */
    int * start;      /**< Array of nb_access start. */
    int * length;     /**< Array of nb_access length. */
};
typedef struct osl_extbody  osl_extbody_t;
typedef struct osl_extbody* osl_extbody_p;

```

### 3.4.7 Loop Extension

#### Description

- URI: loop.
- Author: Taj Muhammad Khan <taj.khan@inria.fr>.
- Purpose: the loop extension provides a means to transfer information about loops in the original code. It starts with the number of loops in the SCoP. For each loop it records: the iterator name, the number of statements, the statement identifiers, the names of private variables, and an identifier for OpenMP pragma directive.

#### File Format

The coordinates extension file format respects the following grammar:

```

Loop_generic      ::= "<loop>" Num_loops Loop_list "</loop>"
Num_loops         ::= _Integer
Loop_list         ::= Loop Loop_list | (void)
Loop              ::= Iterator_name Nb_stmts Stmt_list
                   Private_variables Directive
Iterator_name     ::= _String
Nb_stmts         ::= _Integer
Stmt_list        ::= Stmt_id Stmt_list | (void)
Stmt_id          ::= _Integer
Private_variables ::= _String
Directive        ::= _Integer

```

With in the tags, the number of loops is provided on the first line. Next comes a series of loop structures. Within each loop, the first line contains the name of the iterator, next comes the number of statements in the loop followed by their identifiers separated by spaces. Next line contains the names of the private variables and in the end is the OpenMP pragma directive. In case there are no private variables to be declared for a loop, the special string "(null)" should replace their declaration as shown below.

For instance, the following example is a correct textual loop extension containing two loops:

```
<loop>
# Number of loops
2
# =====
# Loop number 1
# Iterator name
t2
# Number of stmts
1
# Statement identifiers
1
# Private variables
lbv,ubv
# Directive
1
# =====
# Loop number 2
# Iterator name
t2
# Number of stmts
1
# Statement identifiers
2
# Private variables
(null)
# Directive
1
</loop>
```

The pragma directive can have one of the defined values: `OSL_LOOP_DIRECTIVE_NONE`, `OSL_LOOP_DIRECTIVE_PARALLEL`, `OSL_LOOP_DIRECTIVE_MPI`, or `OSL_LOOP_DIRECTIVE_VECTOR`.

### Data Structure

The loop extension data structure is the following:

```
struct osl_loop {
    char * iter;           /* \0 terminated iterator name */
    int  nb_stmts;         /* Number of statements in the loop */
    int * stmt_ids;        /* Array of statement identifiers. */
    char * private_vars;   /* \0 terminated variable names */
    int  directive;        /* the OpenMP directive to implement */
    struct osl_loop * next; /* pointer to the next element */
};
typedef struct osl_loop  osl_loop_t;
typedef struct osl_loop * osl_loop_p;
```

## 3.4.8 Pluto unroll Extension

### Description

- URI: `pluto_unroll`.
- Author: L  na  c Bagn  res <l  naic.bagneres@inria.fr>.



- Purpose: the `pluto_unroll` extension provides a means to transfer unroll information from Pluto in the SCoP. Pluto saves the iterator name, if unroll-and-jam or not and the unroll factor for several loops.

### File Format

The `pluto_unroll` extension file format respects the following grammar:

```

Pluto_unroll  ::= "<pluto_unroll>" Is_present Data_list "</pluto_unroll>"
Is_present    ::= _Integer
Iterator_name ::= _String
Is_Jam        ::= _Integer
Factor        ::= _Integer
Data          ::= Iterator_name Is_Jam Factor Is_present
Data_list     ::= Data_list Data | (void)

```

With in the tags, the first line indicates if data are provided. Next comes three lines: iteraror name, integer to know if jam or not and the unroll factor. Next line indicates if new data are provided, etc.

For instance, the following example is a correct `pluto_unroll` extension containing two unrolls:

```

<pluto_unroll>
1
# Iterator name
t3
# Jam
1
# Factor
4
# Next
1
# Iterator name
t4
# Jam
0
# Factor
4
# Next
0
</pluto_unroll>

```

### Data Structure

The `pluto_unroll` extension data structure is the following:

```

struct osl_pluto_unroll {
    char*      iter;          /* \0 terminated iterator name */
    bool       jam;           /* true if jam, false otherwise */
    unsigned int factor;      /* unroll factor */
    struct osl_pluto_unroll * next; /* next { iter, jam, factor } */
};
typedef struct osl_pluto_unroll  osl_pluto_unroll_t;
typedef struct osl_pluto_unroll * osl_pluto_unroll_p;

```

#### 3.4.9 Irregular Extension

### 3.5 History

OpenScop is a follow-up of Louis-Noël Pouchet et al.'s ScopLib effort which was itself based on Cédric Bastoul et al.'s Clan tool. People involved in OpenScop's genesis are:

- Cédric Bastoul
- Uday Bondhugula
- Tobias Grosser
- Louis-Noël Pouchet
- Sven Verdoolaege

## 4 OpenScop Library

The OpenScop Library, or OSL for short, is an example implementation of the OpenScop specification. Its API is not part of the OpenScop specification. It offers basic functionalities to manipulate the OpenScop data structures (allocate, free, copy, dump, etc.) and file format (read, print, etc.). The OpenScop Library is *not* a polyhedral library. OpenScop is an exchange format, and the OpenScop Library reflects this.

It is a Free Software using the 3-clause BSD License. Programmers should feel free to use it or copy/paste its code in any project, Open Source or not<sup>1</sup>.

### 4.1 Precision

The OpenScop specification does not impose a specific type for the constraint matrix elements. For a maximum flexibility, the OpenScop Library offers an hybrid precision implementation. It supports 32 bits, 64 bits and multiple precision (relying on GNU GMP) relations transparently. At relation allocation time, users have two ways to set the precision. The first way is to call an allocation function with a precision parameter. The second way is to rely on the environment variable `OSL_PRECISION`. The accepted values for this variable are 32 for 32 bits precision, 64 for 64 bits precision and 0 for multiple precision. When this variable is set, its value becomes the default precision for relation elements. For instance, to ensure the OpenScop Library will use 64 bits precision by default, the user may set:

```
export OSL_PRECISION=64
```

if his shell is, e.g., bash or

```
setenv OSL_PRECISION 64
```

if his shell is, e.g., tcsh. The user should add this line to his `.bashrc` or `.tcshrc` (or whatever convenient file) to make this setting permanent.

The OpenScop Library provides the following function to know whether or not a given precision type is supported by the library or not:

```
int osl_int_is_precision_supported(int precision);
```

this function returns 1 if the precision type is supported, 0 otherwise. Possible values for the `precision` parameter are 32 for 32 bits (single) precision, 64 for 64 bits (double) precision and 0 for multiple precision.

### 4.2 Base Functions

The OpenScop Library provides, for each OpenScop data structure, a set of functions devoted to basic manipulation, conversion from file format to data structures and from data structures to file format. The naming convention is consistent for all data structures. Hence, the function prototypes differ only with the name of the data structure. In the following, we will use the generic term of *structure* to refer at any OpenScop data structure. For instance the `osl_structure_malloc()` function is a generic name can be instantiated to `osl_relation_malloc()` or `osl_statement_malloc()` etc.

We present in this documentation only the main functions. Many other utility functions are provided to ease OpenScop format manipulation. The reader is invited to refer at the technical documentation to learn everything about the OpenScop Library.

---

<sup>1</sup> Closed source projects should consider to provide some OpenScop file input and output, so they can be incorporated to any OpenScop-based tool chain.

### 4.2.1 Dumping: `osl_structure_dump` and `idump`

```
void osl_structure_dump(FILE* output, osl_structure_p s);
void osl_structure_idump(FILE* output, osl_structure_p s, int i);
```

Each OpenScop data structure has a dumping functions as shown above. Dumping means writing down the content of the data structure pointed by `s` (and its fields recursively) in a textual form to the `output` file (the file, possibly `stdout`, has to be open for writing). The textual form is not the OpenScop file format but another representation closer to the internal representation in memory and mainly intended for debugging purpose. The `idump` function has an additional integer parameter which corresponds to an indentation level.

### 4.2.2 Printing: `osl_structure_print`

```
void osl_structure_print(FILE* output, osl_structure_p s);
```

Each OpenScop data structure has a pretty printing function as shown above. It prints the content of the data structure pointed by `s` (and its fields recursively) according to the OpenScop file format (see Section 3.2 [OpenScop File Format Specification], page 18) to the `output` file (the file, possibly `stdout`, has to be open for writing).

### 4.2.3 Reading: `osl_structure_read`

```
osl_structure_p osl_structure_read(FILE* input);
```

Each OpenScop data structure has a reading function as shown above. It reads the content of an OpenScop data structure written according to the OpenScop file format (see Section 3.2 [OpenScop File Format Specification], page 18) from the `input` file (the file, possibly `stdin`, has to be open for reading). It returns a pointer to a freshly allocated `osl_structure_t` structure containing the information.

### 4.2.4 Allocating: `osl_structure_malloc`

```
osl_structure_p osl_structure_malloc();
```

Each OpenScop data structure has a memory allocation function as shown above (except one see below). It allocates the memory to store the corresponding data structure, it initializes the pointer fields to `NULL` and the integer fields to `OSL_UNDEFINED` (-1) and it returns a pointer to the allocated space.

An exception to this base description is the `osl_relation_malloc()` function which requires two parameters: the number of rows and columns of the constraint matrix (see Section 3.2.1 [Relations], page 19):

```
osl_relation_p osl_relation_malloc(int nb_rows, int nb_columns);
```

The precision of the relation elements will depend on the `OSL_PRECISION` environment variable (see Section 4.1 [Precision], page 39) if it is set, or the maximum available precision if it is not set. Another allocation function is provided to explicitly set a given precision:

```
osl_relation_p osl_relation_pmalloc(int precision,
                                     int nb_rows, int nb_columns);
```

The `precision` field may take the following values:

- `OSL_PRECISION_SP` for 32 bits precision,
- `OSL_PRECISION_DP` for 64 bits precision,
- `OSL_PRECISION_MP` for multiple precision,

### 4.2.5 Deallocating: `osl_structure_free`

```
void osl_structure_free(osl_structure_p s);
```

Each OpenScop data structure has a memory deallocation function as shown above. It recursively frees the memory allocated for the structure pointed by `s`, i.e., internal structures are also freed.

#### 4.2.6 Cloning: `osl_structure_clone`

```
osl_structure_p osl_structure_clone(osl_structure_p s);
```

Each OpenScop data structure has a clone function as shown above. It recursively copies the content of the structure pointed by `s`, i.e., internal structures are also copied. It returns a pointer to the clone of the structure pointed by `s`.

#### 4.2.7 Testing: `osl_structure_equal`

```
int osl_structure_equal(osl_structure_p s1, osl_structure_p s2);
```

Each OpenScop data structure has a testing function as shown above. It checks whether two pointers are referring to equivalent structures (either by pointing to the same structure or to different structures which contain the same information). It returns 1 if the pointed structures are equivalent, 0 otherwise. This test is *content-based* and is intended for debugging purpose. It is not (and will never be) able to state, e.g., that two relations with different constraint matrices are actually representing the same relation.

### 4.3 Example of OpenScop Library Utilization

Here is a basic example showing how it is possible to use the OpenScop Library, assuming that a standard installation has been done. The following C program reads an OpenScop file from the standard input and dumps the content of the data structures to the standard output.

```
/* example.c */
# include <stdio.h>
# include <osl/osl.h>

int main() {
    osl_scop_p scop;

    // Read the OpenScop file.
    scop = osl_scop_read(stdin);

    // Dump the content of the scop data structure.
    osl_scop_dump(stdout, scop);

    // Save the planet.
    osl_scop_free(scop);

    return 0;
}
```

The compilation command could be:

```
gcc example.c -losl -o example
```

A calling command with the input file test.scop could be:

```
more test.scop | ./example
```

### 4.4 Installation

### 4.4.1 License

First of all, it would be very kind to refer the present document in any publication that results from the use of the OpenScop specification or library, see [Bas11], page 47, (a bibtex entry is provided behind the title page of this manual, along with the copyright notice). The OpenScop Library is provided under the 3-clause BSD license:

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### 4.4.2 Requirements

The OpenScop Library is a stand-alone library. For a basic use, it does not need any additional tool or library. Anyway, to be able to work in conjunction with other tools that manipulate multiple precision numbers, the GNU GMP library can be used as an option.

#### 4.4.2.1 GMP Library (optional)

To be able to deal with insanely large coefficient, the user will need to install the GNU Multiple Precision Library (GMP for short) version 4.2.2 or above<sup>2</sup>. The user can compile it by typing the following commands on the GMP root directory:

- `./configure`
- `make`
- And as root: `make install`

The GMP default installation is `/usr/local`. This directory may not be inside the user's library path. To fix the problem, the user should set

```
export LD_LIBRARY_PATH=$LD_LIBRARY_PATH:/usr/local/lib
```

if your shell is, e.g., `bash` or

```
setenv LD_LIBRARY_PATH $LD_LIBRARY_PATH:/usr/local/lib
```

if your shell is, e.g., `tcsh`. Add the line to your `.bashrc` or `.tcshrc` (or whatever convenient file) to make this change permanent. Another solution is to ask GMP to install in the standard path by using the prefix option of the configure script: `'./configure --prefix=/usr'`.

---

<sup>2</sup> <http://www.swox.com/gmp>

The OpenScop Library has to be built using the GMP library by specifying the convenient configure script options to build the GMP version (see Section 4.4.4 [Optional Features], page 43).

### 4.4.3 Installation Instructions

Once downloaded and unpacked (e.g. using the `'tar -zxvf openscop-0.9.0.tar.gz'` command), you can compile the OpenScop Library by typing the following commands on the OpenScop Library's root directory:

- `./autogen.sh`
- `./configure`
- `make`
- And as root: `make install`

The program binaries and object files can be removed from the source code directory by typing `make clean`. To also remove the files that the `configure` script created (so you can compile the package for a different kind of computer) type `make distclean`.

### 4.4.4 Optional Features

The `configure` shell script attempts to guess correct values for various system-dependent variables and user options used during compilation. It uses those values to create the `Makefile`. Various user options are provided by the OpenScop Library's `configure` script. They are summarized in the following list and may be printed by typing `./configure --help` in the OpenScop Library top-level directory.

- By default, the installation directory is `/usr/local`: `make install` will install the package's files in `/usr/local/bin`, `/usr/local/lib` and `/usr/local/include`. The user can specify an installation prefix other than `/usr/local` by giving `configure` the option `--prefix=PATH`.
- By default, The OpenScop Library supports 32 bits, 64 bits and GMP if it is installed in the standard locations. Using the `--with-gmp` option of `configure` the user can specify that no GMP (`--with-gmp=no`), a previously installed (`--with-gmp=system`, the default) GMP or a build GMP (`--with-gmp=build`) GMP should be used. In case of an installed GMP, the installation location can be specified using the `--with-isl-prefix=PATH` and if different, the installation of the library can be specified using the `--with-isl-exec-prefix=PATH` options of `configure`. In the case of a build GMP, the user can also specify the build location using `--with-isl-builddir=PATH`.

### 4.4.5 Uninstallation

The user can easily remove the OpenScop Library from his system by typing (as root if necessary) from the OpenScop Library top-level directory `make uninstall`.

## 4.5 Documentation

The OpenScop Library distribution provides several sources of documentation. First, the source code itself is as documented as much as possible. The code comments use the Doxygen technical documentation system. The user may install Doxygen<sup>3</sup> to automatically generate a technical documentation by typing `make doc` or `doxygen ./autoconf/Doxyfile` at the OpenScop Library top-level directory after running the `configure` script (see Section 4.4.3 [Installation Instructions], page 43). Doxygen will generate documentation sources (in HTML, LaTeX and man) in the `doc/source` directory of the OpenScop Library distribution.

The Texinfo source of the present document is also provided in the `doc` directory. The user can build it in either PDF format (by typing `texi2pdf openscop.texi`) or HTML format (by

<sup>3</sup> <http://www.stack.nl/~dimitri/doxygen>

typing `makeinfo --html openscop.texi`, using `--no-split` option to generate a single HTML file) or info format (by typing `makeinfo openscop.texi`).

## 4.6 Development

### 4.6.1 Copyright Issue

The OpenScop Library is an Open Source project and you should feel free to contribute by adding functionalities (in particular extensions), correcting bugs or improving documentation. However, for painful administrative reasons, the copyright of the core part (everything except extensions) should not be impacted by your work. Hence, if you are doing a significant contribution to the main part, the OpenScop Library maintainer may ask you for an agreement about this copyright. If you plan to do such a significant contribution, it may be wise to discuss this issue with the maintainer first. Extensions may include developer's own copyright.

### 4.6.2 Repository

The main repository of the OpenScop Library is <http://repo.or.cz/w/openscop.git>. Developers may ask the OpenScop Library maintainer to open them a write access to this repository. Only the maintainer should ever change the `master` branch. Developers should work on their own branches. To avoid any problem developers should use the *fork* functionality of the repository.

### 4.6.3 Coding Style

The OpenScop Library is written in C using an object oriented style. Each important data structure (e.g., `struct foo`) has its own header file (`include/osl/foo.h`) where lies the definition of the data structure, the two typedefs for the data structure (one for the structure, `osl_foo_t`, and one for a pointer to the structure, `osl_foo_p`), the prototypes of the various functions related to this data structure, all named using the prefix "`osl_foo_`". The source code of the functions is provided in a separated C file (`source/foo.c`).

Utility functions independent from the main data structures may be placed in separate source files (e.g., definition in `include/osl/util.h` and code in `source/util.c`). Tool-wide preprocessor directives are placed in `include/osl/macros.h`, macros are prefixed with "`OSL_`".

The core code itself has to be written according to the Google C++ Coding Style: <http://google-styleguide.googlecode.com/svn/trunk/cppguide.xml> (for what can apply to C), plus the naming conventions discussed above with highest priority. The extension parts must only respect the naming convention, but a consistent coding style is much appreciated.

### 4.6.4 Extension Development

It's fairly easy to integrate a new extension to OpenScop and the OpenScop Library. Developing a new extension is very much like adding a new "object": it requires writing a data structure for the extension data and the 7 base functions to manage this extension. Here is how developers should proceed to add an extension called `foo` (beware that the naming convention is strict):

1. Send the name `foo` to the maintainer to ensure it is unique and hence can be used as an URI. The name (one single word, or words separated with underscores "`_`") should be suggested by the extension developers to the OpenScop development mailing list [openscop-development@googlegroups.com](mailto:openscop-development@googlegroups.com)). It should not correspond to an existing structure name (see `include/osl/osl.h` for the list). The maintainer will update `include/osl/osl.h` in the development version accordingly.
2. Look at the `comment` extension. The `comment` extension (see Section 3.4.1 [Comment Extension], page 31) has been written to be used as a basic example for extension developers. Having a look at `include/osl/extensions/comment.h` and `source/extensions/comment.c` will be a great help to do it right.



3. Create the extension data structure: it is necessary that the extension data can be accessible through only one pointer.
4. Code the 7 base functions for the extension. Any extension must provide this set of functions (naming convention apply only if the extension is planned to be integrated to the OpenScop Library default extensions):

- `osl_foo_idump` (see Section 4.2.1 [Dumping], page 40)
- `osl_foo_sprint` has the following prototype:

```
char * osl_structure_sprint(osl_structure_p s);
```

It corresponds to the pretty printing functions of the core data structures (see Section 4.2.2 [Printing], page 40) with the difference that the OpenScop textual representation is written to a string (returned by the function) instead of a file.

- `osl_foo_sread` has the following prototype:

```
osl_structure_p osl_structure_sread(char ** string);
```

It corresponds to the reading functions of the core data structures (see Section 4.2.3 [Reading], page 40) with the difference that the OpenScop textual representation is read from a string (provided as a parameter) instead of a file. The address of the string to read is passed as a parameter and is updated to point immediately after what has been actually read.

- `osl_foo_malloc` (see Section 4.2.4 [Allocating], page 40)
- `osl_foo_free` (see Section 4.2.5 [Deallocating], page 40)
- `osl_foo_clone` (see Section 4.2.6 [Cloning], page 41)
- `osl_foo_equal` (see Section 4.2.7 [Testing], page 41)

5. Code the other functions you need!

Now let us consider two scenarios.

First scenario, the extension is external and is not planned to be integrated to the OpenScop Library. In this case you are all set. Simply generate an `osl_interface_t` for your extension and have a look at the function `osl_scop_register_extension()` which is devoted to register a new extension interface to an existing `osl_scop_t`.

Second scenario, the extension will integrate the set of default OpenScop Library extensions (the best solution to share it to other potential users). In this case, a few additional things have to be done:

1. Create the extension header `include/osl/extensions/foo.h` to store the extension structure and function prototypes and the extension source file `source/extensions/foo.c` for the code of the functions.
2. Add the documentation for the extension to the texinfo source of this document (in `doc/openscop.texi`), following the example of the `comment` documentation (see Section 3.4.1 [Comment Extension], page 31).
3. Integrate the extension by adding the `extensions/foo.c` entry to the `libosl_la_SOURCES` in the `source/Makefile.am` file, the `osl/foo.h` entry to the `nobase_pkginclude_HEADERS` and add the corresponding `#include <osl/extensions/foo.h>` in the `include/scop.h.in` file.
4. Add the new extension in the `osl_interface_get_default_registry()` function.
5. You are done! Prepare a single commit or patch corresponding to the integration of the new extension and ask the maintainer to merge it to the master branch.



## 5 References

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